

4.43

Let us use superposition principle!

- ① Turn off v_2, v_3 : circuit acts like an inverting amplifier, thus:

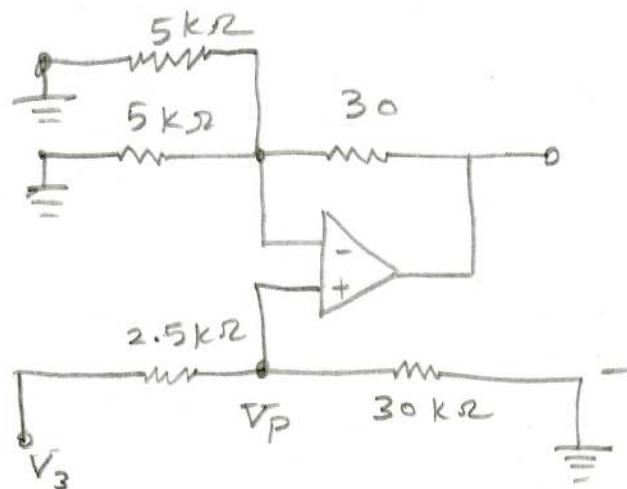
$$V_{o,1} = - \frac{R_F}{R_{in}} V_1 = - \frac{30}{5} V_1 = -6 V_1$$

- ② Turn off V_1, V_3 :

Circuit acts like inverting amp.

$$V_{o,2} = - \frac{R_F}{R_{in}} V_2 = - \frac{30}{5} V_2 = -6 V_2$$

- ③ Turn off V_1, V_2 : circuit acts like non-inverting amplifier:



by voltage division:

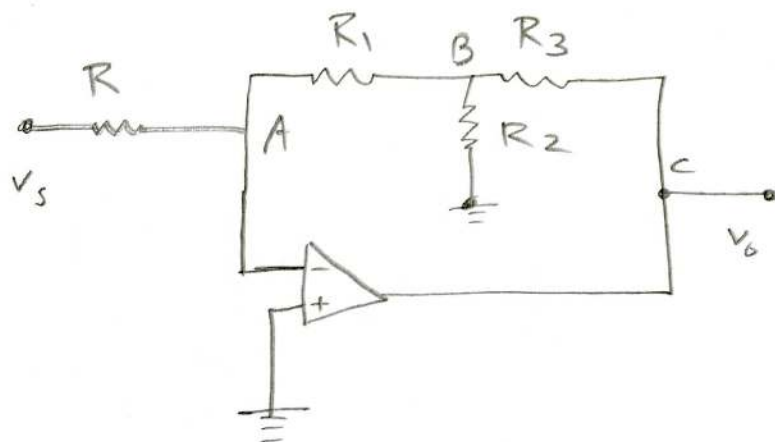
$$V_P = \frac{30}{30+2.5} V_3 = \frac{30}{32.5} V_3$$

Noninverting amplifier;

$$V_{o,3} = \frac{2.5+30}{2.5} V_P = 12 V_3$$

$$V_o = V_{o,1} + V_{o,2} + V_{o,3} = -6 V_1 - 6 V_2 + 12 V_3$$

4.50



This is neither an inverting nor a non-inverting op-Amp
to use node voltage analysis to solve problem

$$\text{KCL at (A)} \quad \frac{V_A - V_s}{R} + \frac{V_A - V_B}{R_1} = 0$$

$$\text{KCL at (B)} \quad \frac{V_B - V_A}{R_1} + \frac{V_B - V_C}{R_3} + \frac{V_B}{R_2} = 0$$

equation of an ideal op-amp $V_A = 0$

now 3-equations / 3 unknowns

$$V_A = 0 \rightarrow V_B = V_s \cdot \frac{-R_1}{R}$$

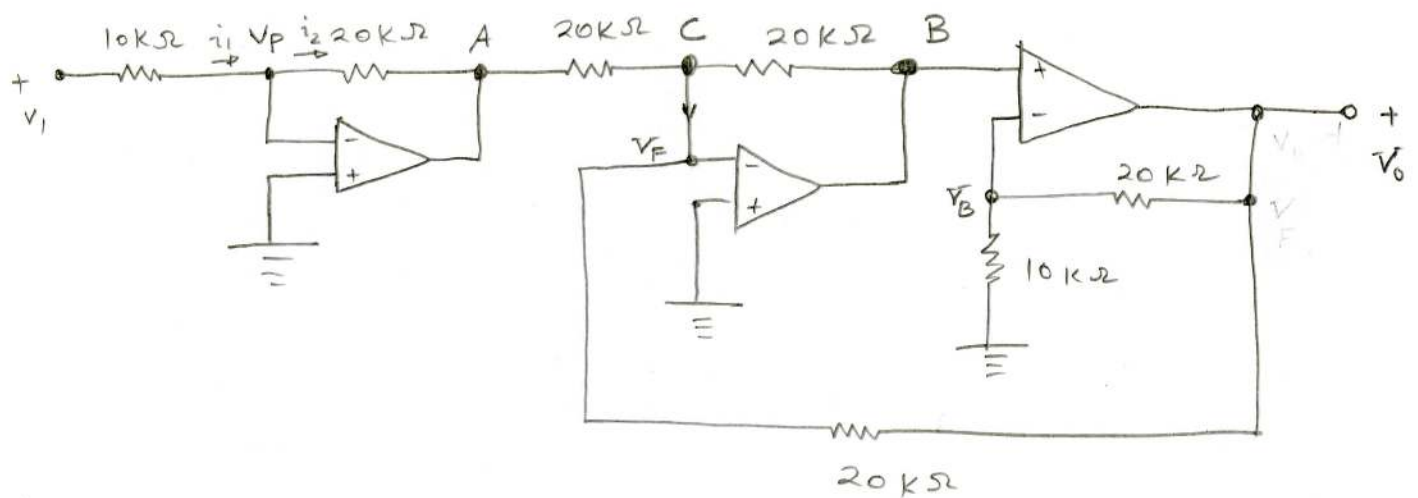
$$V_C = V_s \cdot \frac{-R_1 R_2 - R_1 R_3 - R_2 R_3}{R R_2}$$

$$K = \frac{-R_1 R_2 - R_1 R_3 - R_2 R_3}{R R_2}$$

For $K = -10 \rightarrow$ multiple answers are possible!

4.61

Let us try to find V_A, V_B, V_C



$$i_1 = i_2 \rightarrow \frac{V_1 - V_p}{10} = \frac{V_p - V_A}{20} \quad \xrightarrow[\substack{\text{but} \\ V_p = 0}]{} \frac{V_1 - 0}{10} = \frac{0 - V_A}{20} \rightarrow \boxed{V_A = -2V_1}$$

Also since $V_F = 0$

$$(\text{noninverting amp}) \quad \frac{V_0}{V_B} = \frac{20+10}{10} = 3 \rightarrow \boxed{V_0 = 3V_B}$$

$$\text{writing KCL for } \textcircled{C} \quad \frac{V_F - V_0}{20} = \frac{V_A - V_C}{20} + \frac{V_B - V_C}{20}$$

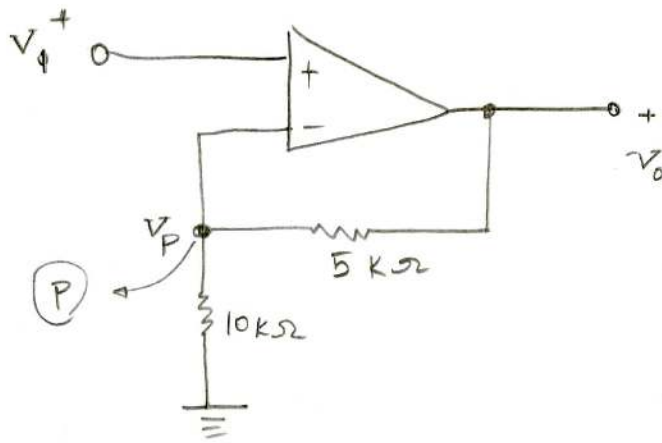
$$\text{and we know } V_F = 0 \rightarrow$$

$$0 - V_0 = V_A + V_B - 2V_C \rightarrow \boxed{2V_C = V_A + V_B + V_0} \quad \text{but } V_C = 0$$

$$\Rightarrow (-2V_1) + \frac{1}{3}V_0 + V_0 = 0 \rightarrow 2V_1 = \frac{4}{3}V_0 \rightarrow$$

$$\boxed{\frac{V_0}{V_1} = \frac{3}{2}}$$

4.61



$$V_1 = V_P$$

at node (P)

$$\frac{V_P - 0}{10} = \frac{V_0 - V_P}{5} \rightarrow \frac{V_1}{10} = \frac{V_0 - V_1}{5}$$

$$V_1 = 2V_0 - 2V_1 \rightarrow 3V_1 = 2V_0 \rightarrow \frac{V_0}{V_1} = \frac{3}{2}$$

$$4.70$$

$$R_2 = 10 R_F$$

$$\text{if put } \frac{R_3 + R_4}{R_4} < 10^{+4} < 10^{+4}$$

Let

$$1001 = \frac{R_3 + R_4}{R_4} = \frac{R_3}{R_4} + 1 \Rightarrow \frac{R_3}{R_4} = 1000 \rightarrow R_3 = 1000 \Omega$$

$$R_4 = 1 \Omega$$

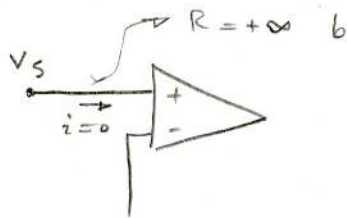
$$\frac{R_F}{R_1} = 3.496 \times 10^{-9} \rightarrow R_F = 3.49 \Omega \quad R_1 = 10^9 \Omega$$

$$\frac{R_F}{R_2} = \frac{1}{10} \rightarrow R_2 = 34.9 \Omega$$

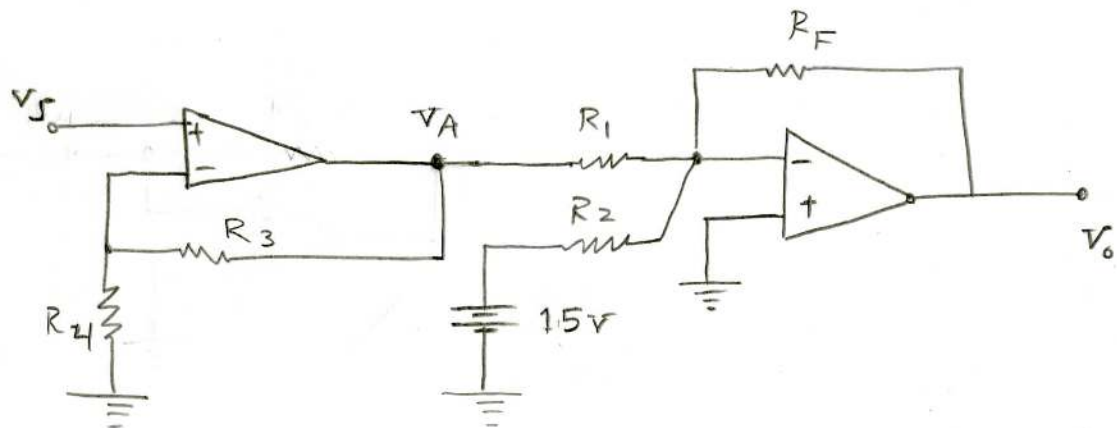
Since input resistance to v_s is infinite

because no current, so it is greater than

$1 \text{ k}\Omega$



4.70



$$\frac{V_O}{V_A} = K_1 = -\frac{R_F}{R_1}$$

$$K_2 = -\frac{R_F}{R_2} = \frac{V_O}{15}$$

$$\Rightarrow \boxed{\frac{V_O}{15} = -\frac{R_F}{R_2}}$$

$$\boxed{\frac{V_O}{V_A} = -\frac{R_F}{R_1}}$$

$$\frac{R_F}{R_1} < 10^4$$

$$\boxed{\frac{V_A}{V_S} = \frac{R_3 + R_4}{R_4}} < 10^4$$

$$\text{and } -\frac{R_F}{R_1} \cdot \frac{R_3 + R_4}{R_4} = -3.5 \times 10^{-6}$$

but for summer we have $K_1 V_A + K_2 (15) = V_O$

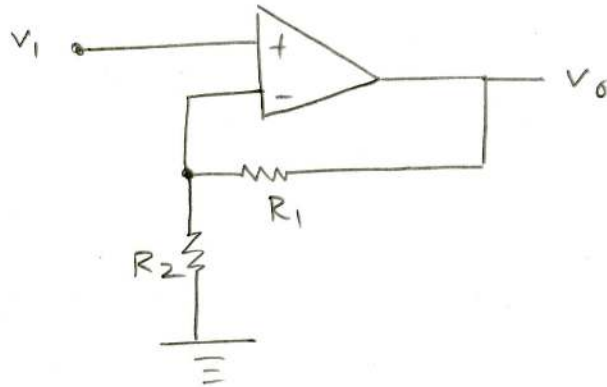
$$V_O = -3.5 \times 10^{-6} V_S + 1.5 = \left(-\frac{R_F}{R_1}\right) V_A + \left(-\frac{R_F}{R_2}\right) 15 \Rightarrow$$

$$V_O = -3.5 \times 10^{-6} V_S - 1.5 = \left(-\frac{R_F}{R_1}\right) \left(\frac{R_3 + R_4}{R_4}\right) V_S + \left(-\frac{R_F}{R_2}\right) 15$$

$$\Rightarrow +\frac{R_F}{R_2} = \frac{1}{10}$$

$$\boxed{\frac{R_F}{R_1} \cdot \frac{R_3 + R_4}{R_4} = 3.5 \times 10^{-6}}$$

4.87



non-inverting
amp.

So we know $\frac{V_0}{V_1} = \left(\frac{R_1 + R_2}{R_2} \right)$

but when $pH = 4$, then $V_1 = 4 \times 50 \text{ mV} = 0.2 \text{ V}$

when $pH = 7$ then $V_1 = 7 \times 50 \text{ mV} = 0.35 \text{ V}$

and for $V_1 = 0.2 \text{ V}$ we have $V_0 = 1 \text{ V}$

$V_1 = 0.35 \text{ V}$ we have $V_0 = 1.75$

So $K = \frac{1}{0.2} = \frac{1.75}{0.35} = 5$

$\frac{R_1 + R_2}{R_1} = 5 \rightarrow R_1 = 2 \text{ k}\Omega, R_2 = 8 \text{ k}\Omega$