

4.4) $\frac{V_o}{V_s} = ?$ and $\frac{i_o}{i_x} = ?$

From $V = i \cdot R$, $i_x = \frac{V_s}{1.0k\Omega}$

Again from Ohm's Law $V_o = -50 i_x \cdot 2.2k\Omega$

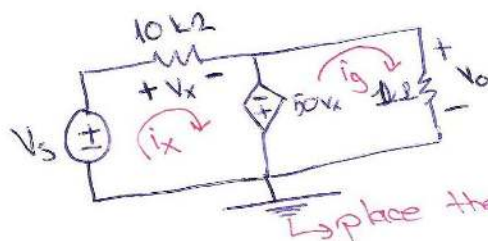
Substituting i_x , we get

$$V_o = -165 V_s \Rightarrow \frac{V_o}{V_s} = -165$$

Since the direction of i_o is opposite

$$50 i_x = -i_o \Rightarrow \frac{i_o}{i_x} = -50$$

4.5) $\frac{V_o}{V_s} = ?$



We do mesh analysis

KVL @ mesh X

$$\Rightarrow 10k\Omega i_x - 50V_x - V_s = 0$$

KVL @ mesh Y

$$\Rightarrow 1k\Omega i_o + 50V_x = 0$$

By using Ohm's Law
 $V_x = i_x \cdot (10k\Omega)$

4.5) cont. Substituting V_x into equation,
we get

$$-490k\Omega i_x - V_s = 0$$

$$1k\Omega i_y + 500k\Omega i_x = 0$$

By solving two equations for two unknowns,
we get

$$i_x = -\frac{1}{490k\Omega} V_s$$

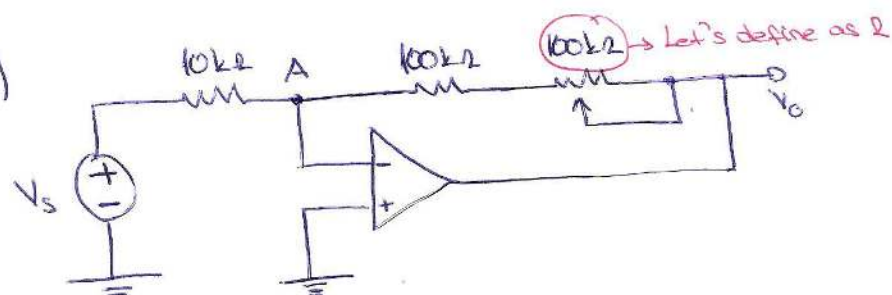
$$i_y = \frac{50}{49k\Omega} V_s$$

By using Ohm's law, we get

$$V_o = i_y \cdot 1k\Omega = \frac{50}{49} V_s$$

$$\Rightarrow \frac{V_o}{V_s} = \frac{50}{49}$$

4.22)



KCL @ node A

(By using OpAmp properties we can find $V_A = 0$)

$$\Rightarrow \frac{V_s}{10k\Omega} + \frac{V_o}{(100+R)k\Omega} = 0$$

$$\frac{V_o}{V_s} = - \frac{(100+R)}{10}$$

for $R=0$

$$\frac{V_o}{V_s} = -10$$

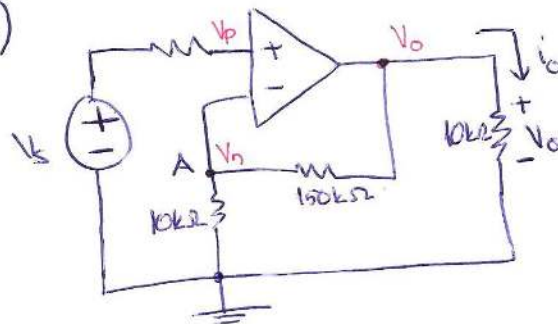
for $R=100$

$$\frac{V_o}{V_s} = -20$$

Then

$$\frac{V_o}{V_s} \in [-20, -10]$$

4.23)



$$V_{cc} = \pm 24V$$

a) Using opAmp Properties, we obtain

$$V_s = V_p = V_n = V_A$$

KCL @ node A

$$-\frac{V_s}{10} + \frac{V_o - V_s}{150} = 0 \Rightarrow$$

$$V_o = 16 V_s$$

b) By using Ohm's Law

$$i_o = \frac{V_o}{10k\Omega}$$

For $V_s = 1$

$$i_o = \frac{16}{10k\Omega} = 1.6mA$$

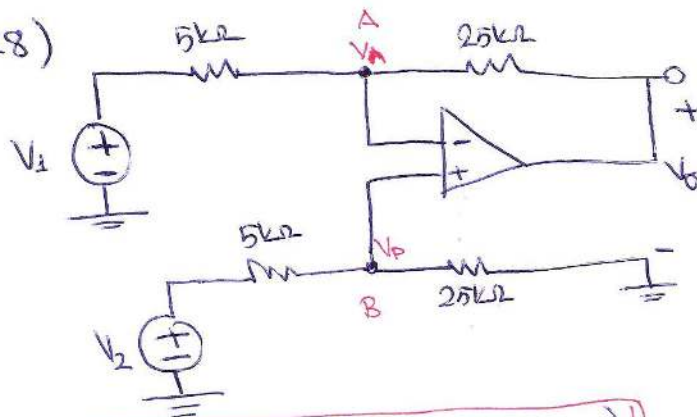
For $V_s = 3$

$$V_o = 24$$

since it is saturated ($V_{cc} = \pm 24V$, remember the graph!)

$$i_o = \frac{24}{10k\Omega} = 2.4mA$$

4.28)



$$V_n = V_p \text{ (property of OpAmp)}$$

* KCL @ node A

$$\frac{V_1 - V_n}{5k\Omega} - \frac{V_n - V_o}{25k\Omega} = 0$$

$$\Rightarrow \frac{5V_1 + V_o}{6} = V_n$$

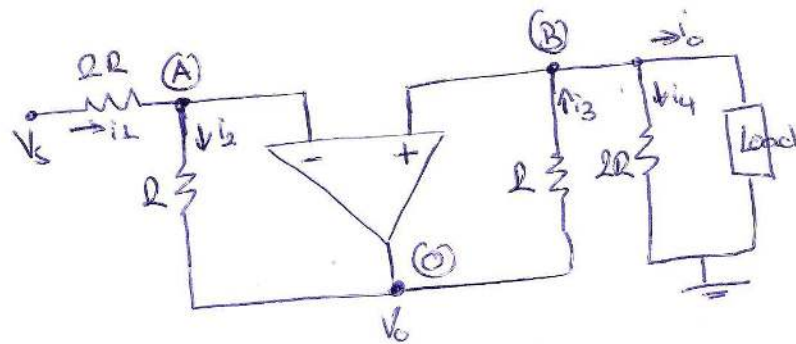
* KCL @ node B

$$\frac{V_2 - V_p}{5k\Omega} - \frac{V_p}{25k\Omega} = 0 \Rightarrow \frac{5V_2}{6} = V_p$$

Since $V_p = V_n \Rightarrow 5V_1 + V_o = 5V_2$

$$\Rightarrow V_o = 5(V_2 - V_1)$$

4.34)



Using property of OpAmp, $V_A = V_B$

* KCL @ node A

$$i_1 - i_2 = 0$$

$$\Rightarrow \frac{V_s - V_A}{2R} - \frac{V_A - V_o}{R} = 0$$

$$\Rightarrow V_A \left(-\frac{3}{2R} \right) + \frac{V_o}{R} = -\frac{V_s}{2R} \quad (1)$$

* KCL @ node B

$$i_3 - i_4 - i_o = 0$$

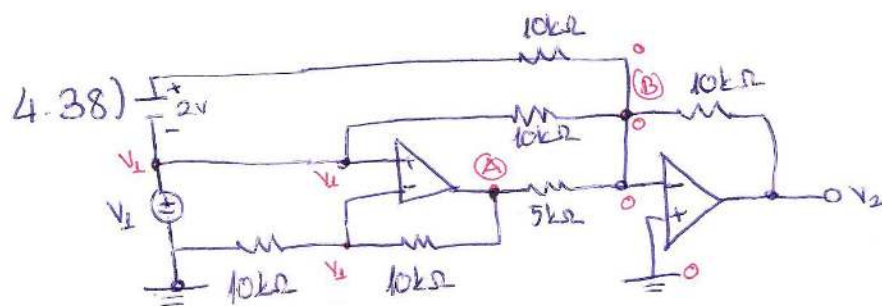
$$\Rightarrow \frac{V_o - V_A}{R} - \frac{V_A}{2R} - i_o = 0$$

$$\Rightarrow V_A \left(-\frac{3}{2R} \right) + \frac{V_o}{R} = i_o \quad (2)$$

4.34) Cont.

Subtracting eqn. (1) from eqn. (2), we get

$$i_o = \frac{-V_s}{2R}$$



By using OpAmp property, $V_B = 0$

* KCL @ node A

$$-\frac{V_A - V_1}{10} - \frac{V_A}{5} = 0 \Rightarrow V_A = -\frac{V_1}{3}$$

KCL @ node B

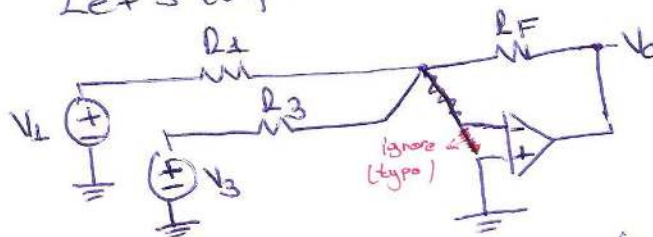
$$\Rightarrow \frac{V_1 + 2}{10} + \frac{V_1}{10} + \frac{V_A}{5} + \frac{V_2}{10} = 0$$

4.38) cont. Substituting $V_A = -\frac{V_1}{3}$ into the equation we get

$$V_2 = -\left(\frac{4}{3}V_1 + 2\right)$$

4.45) We can use one inverting amp and one summing amplifier.

Let's do first summing part



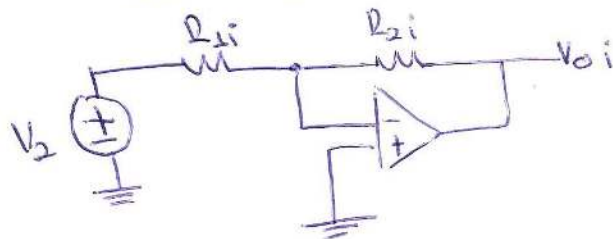
Up to now $V_0 = -\left(\frac{R_F}{R_1}\right)V_1 + \left(-\frac{R_F}{R_3}\right)V_3$

choose

$$\begin{aligned} R_F &= 15 \\ R_1 &= 5 \\ R_3 &= 3 \end{aligned}$$

4.45) cont

Secondly inverting amp.



$$V_{o1} = - \frac{R_{2i}}{R_{1i}} V_2$$

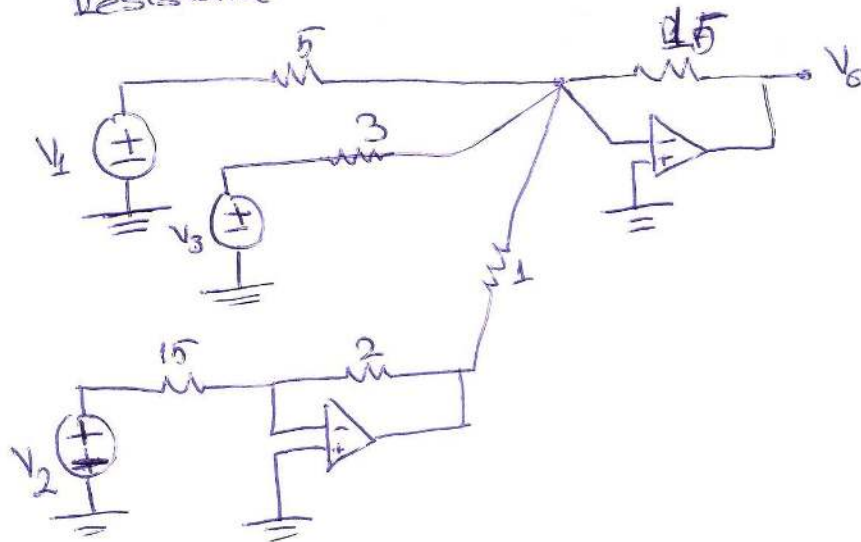
we ~~need~~ can choose

$$R_{1i} = 15$$

$$R_{2i} = 2$$

Combining this two amp with $R=1$

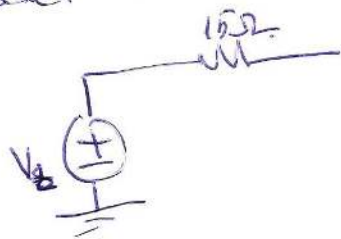
Resistance.



4.55) From the figure, we get the relationship between transducer and temperature. So, it is linear and for 400°C , it gives 30 mV potential. Then linear relation is

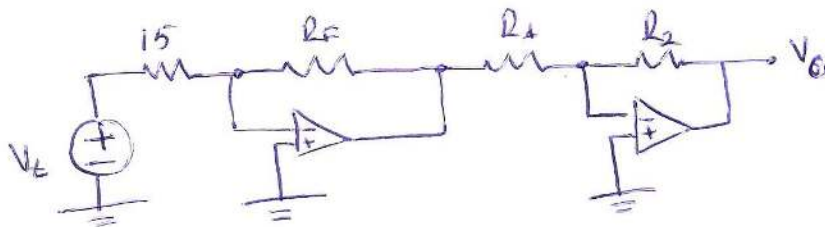
$$0.75 \times 10^{-4} (\text{Temperature } ^{\circ}\text{C}) = (\text{Potential}) \text{ Volt}$$

As it is given in the problem we can model transducer as



Using one sum one inverting amp. we get the circuit as follows:

4.55) cont.

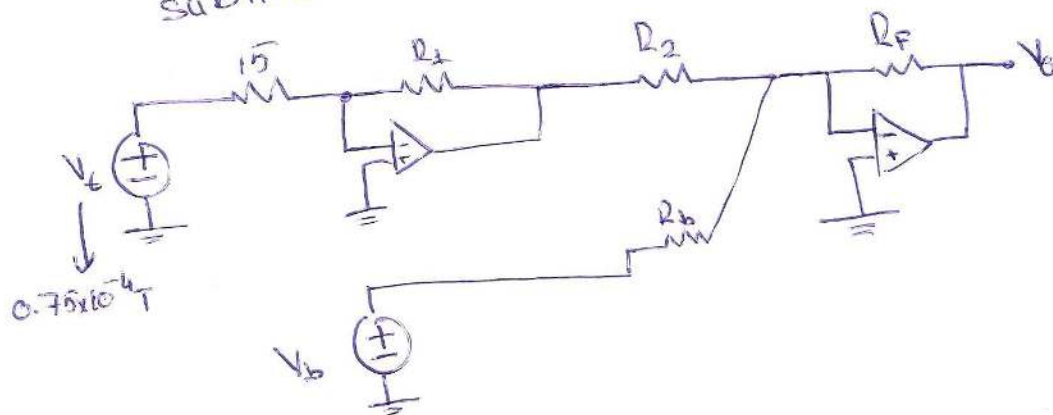


$V_t = 0.75 \times 10^{-4} \text{ V}$ for $T = 1000^\circ\text{C}$ we need to get $V_o = 5 \text{ V}$. Then by choosing $R_1 = R_2$, we can calculate R_F

$$0.075 \left(-\frac{R_F}{15} \right) = -5 \text{ V}$$

$$\Rightarrow R_F = 1000 \Omega$$

4.66) Let's choose some thermocouple as problem. 4.55. For this question, we need to add a bias to the output. To use ~~fewer~~ less OpAmp in the design is ~~to~~ using inverter after thermocouple and then using summation. Since the gain is negative, we will basically do subtraction.



4.66) cont.
T

$$V_t \left(\frac{R_1}{R_2} \right) \left(\frac{R_F}{R_2} \right) - V_b \left(\frac{R_F}{R_b} \right) = V_o$$

$$\begin{array}{ll} \text{When } T = 350^\circ\text{C} & V_o = 0 \\ T = 1100^\circ\text{C} & V_o = 5\text{V} \end{array}$$

$$T = 350^\circ\text{C} \Rightarrow V_t = 262.5 \times 10^{-4} \text{ V}$$

$$T = 1100^\circ\text{C} \Rightarrow V_t = 825 \times 10^{-4} \text{ V}$$

Let's choose.

$$R_1 = 1000$$

$$R_2 = 1 \quad \text{and } V_b = 5\text{V}$$

$$R_b = 2.857$$

$$R_F = 1.26$$

4.66) cont.

Here is the explanation, how we choose

variables.

- * Firstly we choose $R_1 = 1000$, $R_2 = 1$ and $V_b = 5V$, they are in the design range,
- * Now let's calculate V_b for $T = 350^\circ C$

$$R_F \left(262.5 \times 10^{-4} \times \frac{1000}{15} - \frac{5}{R_b} \right) = V_b$$

We need to choose R_b such that $V_o = 0$
so when we solve the equation we get

$$R_b = 2.857.$$

- * Lastly, we solve R_F such that for $T = 1100^\circ C$, $V_b = 5V$, this gives $R_F = 1.26$.