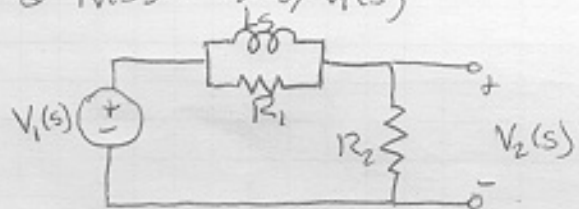


P.11.2 find driving pt. impedance & $T_v(s) = V_2(s)/V_1(s)$

$$Z_{EQ} = R_2 + \frac{R_1 Ls}{R_1 + Ls}$$

$$Z_{EQ} = \frac{(R_1 + R_2)Ls + R_1 R_2}{R_1 + Ls}$$



$$V_2(s) = T_v(s) V_1(s) \rightarrow \text{voltage divider}$$

$$T_v(s) = \frac{R_2}{Z_{EQ}} =$$

$$T_v(s) = \frac{R_2(Ls + R_1)}{(R_1 + R_2)Ls + R_1 R_2}$$

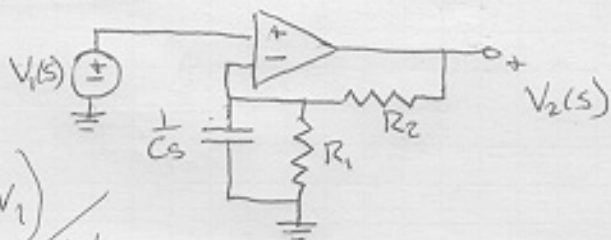
P.11.4 find driving pt. impedance & $T_v(s)$

OP-AMP Golden rule $I_N = I_P = 0$

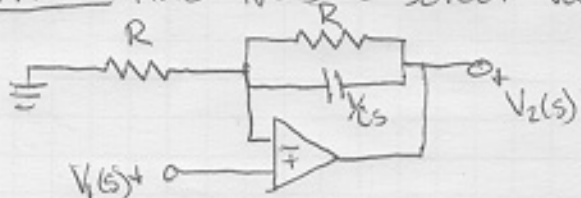
$$\therefore Z_{EQ} = \infty$$

$$T_v(s) = \frac{V_2(s)}{V_1(s)} = \left(\frac{R_2 + \left(\frac{1}{R_1 + Cs} \right) V_1}{\left(\frac{1}{R_1 + Cs} \right)} \right) V_1$$

$$T_v(s) = \frac{R_1 R_2 Cs + R_1 + R_2}{R_1}$$



P.11.7 find $T_v(s)$ & select values of R & C so there is a pole @ $s = -500 \text{ rad/s}$



inverting amplifier

$$T_v(s) = \frac{R}{RCs + 1} + R$$

$$T_v(s) = \frac{RCs + 2}{RCs + 1}$$

any values of R & C
such that

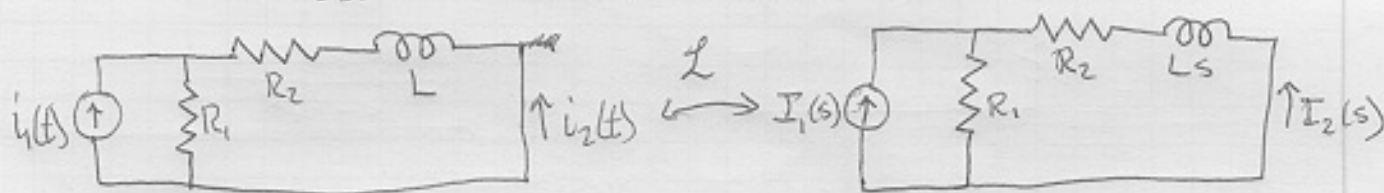
$$RC = \frac{1}{500}$$

ex.

$$R = 1 \text{ k}\Omega$$

$$C = 2 \mu\text{F}$$

P.11.28 If circuit is in steady state with $i_1(t) = 10 \cos 500t$ mA & $R_1 = 100 \Omega$, $R_2 = 400 \Omega$, & $L = 100$ mH
find $i_{2ss}(t)$. Repeat with $i_1(t) = 10 \cos 5000t$ mA



with input $i_1(t) = A \cos(\omega t)$
Steady State output will have the form $i_{ss}(t) = A |T(j\omega)| \cos(\omega t + \theta)$

so what is $T(s) \rightarrow$ use current divider where $\theta = \angle T(j\omega)$

$$T(s) = \frac{\left(\frac{1}{R_2 + Ls} \right)}{\frac{1}{R_1} + \frac{1}{R_2 + Ls}} = \frac{R_1}{Ls + R_1 + R_2} = \frac{R_1/L}{s + \frac{R_1 + R_2}{L}}$$

with given values $T(s) = \frac{1000}{s + 5000}$

$$|T(j500)| = \frac{1000}{\sqrt{500^2 + 5000^2}} = \frac{2}{\sqrt{101}}$$

$$\theta(j500) = 0 - \tan^{-1}\left(\frac{500}{5000}\right)$$

$$i_1(t) = 10 \cos(500t) \text{ mA}$$

$$i_{2ss}(t) = -10 |T(j500)| \cos(500t + \theta) \text{ mA}$$

$$= 10 |T(j500)| \cos(500t + \pi + \theta) \text{ mA}$$

$$i_{2ss}(t) \approx 1.99 \cos(500t + 3.04) \text{ mA}$$

$$i_1(t) = 10 \cos(5000t) \text{ mA}$$

$$|T(j5000)| = \frac{1000}{\sqrt{5000^2 + 5000^2}} = \frac{1}{5\sqrt{2}}$$

$$\theta = 0 - \tan^{-1}\left(\frac{5000}{5000}\right)$$

$$i_{2ss}(t) \approx 10 \frac{1}{5\sqrt{2}} \cos(5000t + \pi + \theta) \text{ mA}$$

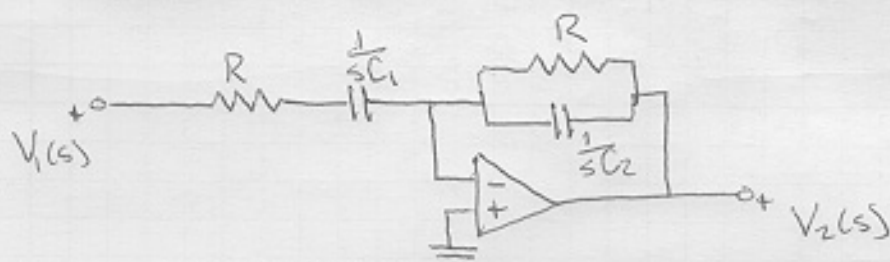
$$i_{2ss}(t) \approx 1.41 \cos(5000t + 2.356) \text{ mA}$$

P.11.53 Design a circuit to fit $T_V(s) = \pm \frac{1000s}{(s+500)(s+1000)}$

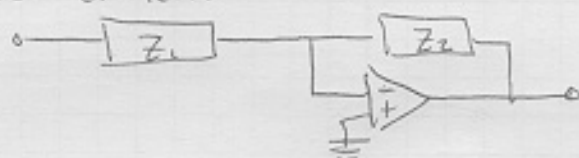
using only resistors, capacitors & not more than one OP-AMP
 - scale it so that the final design uses only $20k\Omega$ resistors

$$T_V(s) = \frac{k_1}{s+500} \frac{k_2 s}{s+1000}$$

ex.



inverting amplifier ~~from~~



$$\text{Gain} = - \frac{Z_2}{Z_1}$$

$$\text{in example } Z_2 = \frac{1}{\frac{1}{R} + sC_2} = \frac{R}{RC_2s + 1}$$

$$Z_1 = R + \frac{1}{sC_1} = \frac{RC_1s + 1}{C_1s}$$

$$T_V(s) = - \frac{Z_2}{Z_1} = - \frac{R}{RC_2s + 1} \frac{C_1s}{RC_1s + 1}$$

$$= - \frac{1}{RC_2} \frac{1}{s + \frac{1}{RC_2}} \frac{s}{s + \frac{1}{RC_1}}$$

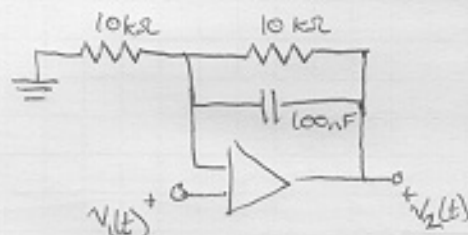
if $R = 20k\Omega$

$C_1 = 100nF$

$C_2 = 50nF$

$$T_V(s) = - \frac{1000s}{(s+500)(s+1000)}$$

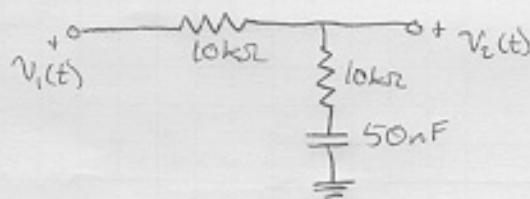
P.11.58 Show that both circuits satisfy the transfer function
 $T_V(s) = K \left(\frac{s+2000}{s+1000} \right)$



non-inverting amplifier
 Gain = $T_V(s) = \frac{R/Cs}{R + 1/Cs} + R$

$$= \frac{R}{RCs + 1}$$

$$T_V(s) = \frac{s + 2000}{s + 1000}$$



voltage divider

$$V_2(s) = \frac{R + 1/Cs}{R + R + 1/Cs} V_1(s)$$

$$T_V(s) = \frac{R + 1/Cs}{2R + 1/Cs}$$

$$= \frac{RCs + 1}{2RCs + 1}$$

$$= \frac{1}{2} \frac{s + 2000}{s + 1000}$$

$$T_V(s) = \frac{1}{2} \frac{s + 2000}{s + 1000}$$

~~Which circuit would you choose to drive a 1k load?~~

b) Which circuit would you choose to drive a 1k load?

OP-AMP circuit

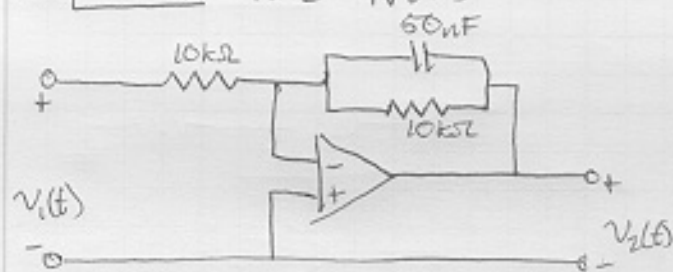
c) Which would you pick if driven by a 50Ω source?

OP-AMP circuit

d) Do you agree with the statement that the transfer function would be $|T_V(s)|^2$ if the two circuits were connected in cascade, regardless of order? Explain.

Yes. Neither order would suffer from loading.

P.12.4) find $T_v(s)$



inverting amplifier

$$T_v(s) = - \frac{\left(\frac{R}{RCs+1} \right)}{R}$$

$$= - \frac{1}{RCs+1}$$

$$T_v(s) = - \frac{1}{RC} \frac{1}{s + 1/RC}$$

$$T_v(s) = - \frac{2000}{s + 2000}$$

a)

$$\text{dc gain} = |T(0)| = 1$$

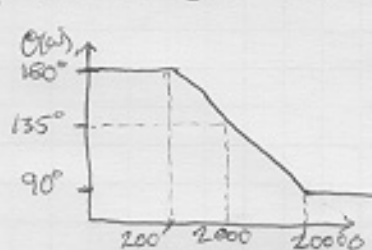
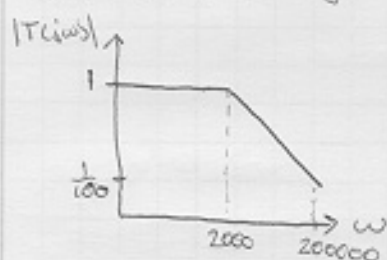
$$\text{Infinite frequency gain} = |T(\infty)| = 0$$

$$\text{cutoff frequency} = \text{absolute value of pole} = 2000 \frac{\text{rad}}{\text{s}}$$

What type of filter is this?

Low-Pass

b) Draw a straight line approx. for gain & phase of $T_v(j\omega)$



$$\theta(\omega) = \pi - \tan^{-1}\left(\frac{\omega}{2000}\right)$$

c) What element values would you change to double the passband gain without changing the cutoff frequency?

have the left most resistor
i.e. make it $5k\Omega$

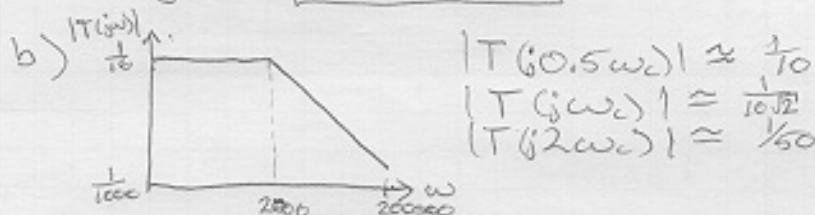
P.12.10 a) Identify the gain response, cutoff frequency & passband gain for $T(s) = \frac{10/s}{100/s + 1/20}$

b) Sketch straight line gain response & estimate the gain for $0.5\omega_c$, ω_c , $2\omega_c$

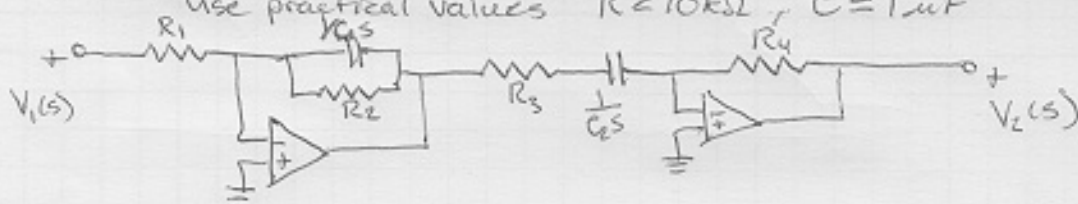
a) $|T(0)| \rightarrow 1/10$
 $|T(\infty)| \rightarrow 0$ Low - Pass

$\omega_c = 2000 \text{ rad/s}$

passband gain $|T(0)| = \frac{1}{10}$



P.12.15 for the circuit, identify the elements that control the two cutoff frequencies & select element values so that the passband gain is 10 & the cutoff frequencies are 100 rad/s & 2500 rad/s .
 Use practical values $R \geq 10 \text{ k}\Omega$, $C \leq 1 \mu\text{F}$



cascade connection of high-pass & low-pass

$$T(s) = T_1(s) \cdot T_2(s)$$

$$T_1(s) = -\frac{R_2}{R_1} \frac{1}{s + \frac{1}{R_2 C_1}} \quad T_2(s) = -\frac{R_4 C_2}{R_3 C_2} \frac{s}{s + \frac{1}{R_3 C_2}}$$

$$T_V(s) = \frac{R_2 R_4}{R_1 R_3} \frac{1}{s + \frac{1}{R_2 C_1}} \frac{s}{s + \frac{1}{R_3 C_2}}$$

$R_2, R_3, C_1, \& C_2$ determine the cutoff frequencies

ex. select

$$R_2 = 10 \text{ k}\Omega, C_1 = 40 \text{ nF} \quad \omega_{c1} = 2500 \text{ rad/s}$$

$$R_3 = 10 \text{ k}\Omega, C_2 = 1 \mu\text{F} \quad \omega_{c2} = 100 \text{ rad/s}$$

take $\omega_{c1} \ll \omega \ll \omega_{c2}$

$$T(j\omega) = \frac{R_4}{R_1} \frac{1}{j\omega} \frac{j\omega}{\omega_{c2}} = \frac{R_4}{R_1} \frac{1}{2500} \stackrel{\text{set}}{=} 10$$

"

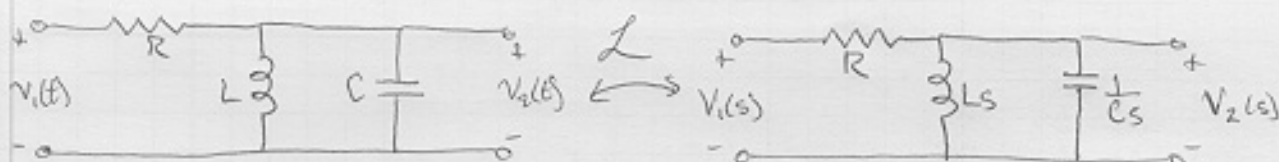
$$R_4 = 2500 R_1$$

choose

$$R_4 = 25 \text{ M}\Omega$$

$$R_1 = 10 \text{ k}\Omega$$

P.12.28 for the bandpass circuit find $T_V(s)$, B , Q , ω_{c1} & ω_{c2} when $R = 50 \Omega$, $L = 50 \mu\text{H}$ & $C = 20 \text{ nF}$



voltage divider

$$V_2(s) = \frac{\left(\frac{1}{Ls} + Cs\right)}{R + \left(\frac{1}{Ls} + Cs\right)} V_1(s) \Rightarrow T_V(s) = \frac{\left(\frac{1}{Ls} + Cs\right)}{R + \left(\frac{1}{Ls} + Cs\right)}$$

$$= \frac{Ls}{RLCs^2 + Ls + R}$$

$$T_V(s) = \frac{1}{RC} \frac{s}{s^2 + \frac{1}{RC}s + \frac{1}{LC}}$$

$$T_V(s) = \frac{1}{R} \frac{1}{Cs + \frac{1}{Ls} + \frac{1}{R}}$$

the cutoff frequencies occur when

$$\left(Cs + \frac{1}{Ls}\right) \Big|_{s=j\omega} = \pm \frac{j}{R}$$

$$\Rightarrow -\omega^2 \pm \frac{1}{RC}\omega + \frac{1}{LC} = 0$$

by quadratic formula

$$\omega_{c1} = -\frac{1}{2RC} + \sqrt{\left(\frac{1}{2RC}\right)^2 + \frac{1}{LC}} \approx 6.18 \times 10^5 \frac{\text{rad}}{\text{s}}$$

$$\omega_{c2} = +\frac{1}{2RC} + \sqrt{\left(\frac{1}{2RC}\right)^2 + \frac{1}{LC}} \approx 1.62 \times 10^6 \frac{\text{rad}}{\text{s}}$$

$$B = \omega_{c2} - \omega_{c1} = \frac{1}{RC} = 10^6 \frac{\text{rad}}{\text{s}}$$

$$Q = \frac{\omega_0}{B} = R\sqrt{\frac{C}{L}} = 1$$